Write your name here


Mathematics A
Level $1 / 2$
Paper 4H
Higher Tier
Sample assessment material for first teaching September 2016
Paper Reference
Time: $\mathbf{2}$ hours
4MA1/4H

## You must have:

Total Marks
Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Calculators may be used.
- You must NOT write anything on the formula page.

Anything you write on the formulae page will gain no credit.

## Information

- The total mark for this paper is 100 .
- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

| Arithmetic series <br> Sum to $n$ terms, $S_{n}=\frac{n}{2}[2 a+(n-1) d]$ | $\text { Area of trapezium }=\frac{1}{2}(a+b) h$ |
| :---: | :---: |
| The quadratic equation <br> The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$ are given by: $x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$ |  |
| Trigonometry | In any triangle $A B C$ <br> Sine Rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$ <br> Cosine Rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$ <br> Area of triangle $=\frac{1}{2} a b \sin C$ |
| Volume of cone $=\frac{1}{3} \pi r^{2} h$ <br> Curved surface area of cone $=\pi r l$ | Volume of prism $=$ area of cross section $\times$ length |
| Volume of cylinder $=\pi r^{2} h$ Curved surface area of cylinder $=2 \pi r h$ | Volume of sphere $=\frac{4}{3} \pi r^{3}$ <br> Surface area of sphere $=4 \pi r^{2}$ |

## Answer ALL TWENTY FIVE questions.

Write your answers in the spaces provided. You must write down all stages in your working.

1 Find the lowest common multiple (LCM) of 20, 30 and 45.

2 The first four terms of an arithmetic sequence are

| 2 | 9 | 16 | 23 |
| :--- | :--- | :--- | :--- |

Write down an expression, in terms of $n$, for the $n$th term.


Diagram NOT
accurately drawn

The diagram shows a solid prism.
The cross section of the prism is a trapezium.
The prism is made from wood with density $0.7 \mathrm{~g} / \mathrm{cm}^{3}$
Work out the mass of the prism.

4
(a) Simplify $p^{5} \times p^{4}$
$\qquad$
(b) Simplify $\left(m^{4}\right)^{-3}$
(c) Write down the value of $c^{0}$
(d) Write $\sqrt[3]{2}$ as a power of 2 .
(e) Solve $5(x+7)=2 x-10$

Show clear algebraic working.

$$
x=
$$

5 On 1 May 2012, the cost of 5 grams of gold was 14000 rupees.
The cost of gold decreased by $7.5 \%$ from 1 May 2012 to 1 May 2013.
Work out the cost of 20 grams of gold on 1 May 2013.
rupees

(a) On the grid, translate triangle $\mathbf{A}$ by the vector $\binom{5}{2}$
(b) Describe fully the single transformation that maps triangle A onto triangle $\mathbf{B}$.
$\qquad$
$\qquad$
$7 a, b, c$ and $d$ are 4 integers written in order of size, starting with the smallest integer.
The mean of $a, b, c$ and $d$ is 15
The sum of $a, b$ and $c$ is 39
(a) Find the value of $d$.

$$
d=
$$

$\qquad$

Given also that the range of $a, b, c$ and $d$ is 10 ,
(b) work out the median of $a, b, c$ and $d$.

8 Kwo invests HK $\$ 40000$ for 3 years at 2\% per year compound interest.
Work out the value of the investment at the end of 3 years.

HK\$.
(Total for Question 8 is $\mathbf{3}$ marks)

9 Solve the simultaneous equations

$$
\begin{aligned}
3 x+y & =13 \\
x-2 y & =9
\end{aligned}
$$

Show clear algebraic working.

$$
\begin{aligned}
& x=. \\
& y=.
\end{aligned}
$$

$\qquad$

10 Show that $4 \frac{2}{3} \div 3 \frac{5}{9}=1 \frac{5}{16}$


Diagram NOT
accurately drawn
$A B C D E F$ is a hexagon.
Work out the value of $y$.

12 The table shows information about the amount of money that 120 people spent in a shop.

| Amount of money (fm) | Frequency |
| :---: | :---: |
| $0<m \leq 10$ | 8 |
| $10<m \leq 20$ | 17 |
| $20<m \leq 30$ | 25 |
| $30<m \leq 40$ | 40 |
| $40<m \leq 50$ | 22 |
| $50<m \leq 60$ | 8 |

(a) Complete the cumulative frequency table.

| Amount of money (£m) | Cumulative frequency |
| :---: | :---: |
| $0<m \leq 10$ |  |
| $0<m \leq 20$ |  |
| $0<m \leq 30$ |  |
| $0<m \leq 40$ |  |
| $0<m \leq 50$ |  |
| $0<m \leq 60$ |  |

(b) On the grid, draw a cumulative frequency graph for your table.

(c) Use your graph to find an estimate for the median amount of money spent in the shop by these people.
$\qquad$

13 Make $b$ the subject of $P=\frac{1}{2} a b^{2}+c$ where $b$ is positive.

14 The line with equation $y=2 x$ is drawn on the grid.
(a) On the same grid, draw the line with equation $4 x+3 y=12$

(b) Show, by shading on the grid, the region defined by all four inequalities

$$
\begin{gathered}
y \leq 2 x \\
4 x+3 y \leq 12 \\
y \geq-3 \\
x \leq 4
\end{gathered}
$$

15 There are 100 students in Year 11
All 100 students study at least one of art, drama and music.
7 of the students study art and drama and music.
23 of the students study art and drama.
35 of the students study art and music.
12 of the students study music and drama.
65 of the students study art.
52 of the students study music.
(a) Draw a Venn diagram to show this information.

One of the 100 students is selected at random.
(b) Find the probability that this student studies Drama but not Music.

Given that the student studies Drama,
(c) find the probability that this student also studies Art.
$16 \quad M$ is inversely proportional to $g^{3}$ $M=24$ when $g=2.5$
(a) Find a formula for $M$ in terms of $g$
(b) Work out the value of $g$ when $M=\frac{1}{9}$

$$
g=.
$$

17 The function f is such that $\mathrm{f}(x)=\frac{3}{x-2}$
(a) Find $f(1)$
$\qquad$
(b) State which value of $x$ must be excluded from any domain of f

The function g is such that $\mathrm{g}(x)=x+4$
(c) Calculate $\mathrm{fg}(2)$
$\qquad$

18 Solid $\mathbf{A}$ and solid $\mathbf{B}$ are mathematically similar.
Solid A has surface area $384 \mathrm{~cm}^{2}$
Solid B has surface area $864 \mathrm{~cm}^{2}$
Solid B has a volume of $2457 \mathrm{~cm}^{3}$
Calculate the volume of solid $\mathbf{A}$.
. $\mathrm{cm}^{3}$

19 Here are nine graphs.

Graph A

Graph D

Graph G

Graph B

Graph E

Graph $\mathbf{F}$

Graph H

Graph C

Graph I

Complete the table below with the letter of the graph that could represent each given equation.

| Equation | Graph |
| :---: | :---: |
| $y=\sin x$ |  |
| $y=2-3 x$ |  |
| $y=x^{2}+x-6$ |  |
| $y=x^{3}+3 x^{2}-2$ |  |

20 Gemma has 9 counters.
Each counter has a number on it.


Gemma puts the 9 counters into a bag.
She takes at random two counters from the bag.
(a) Work out the probability that the number on each counter is an even number.
(b) Work out the probability that the sum of the numbers on the two counters is an odd number. Show your working clearly.

21 Here is triangle $L M N$, where angle $L M N$ is an obtuse angle.


Diagram NOT accurately drawn

Work out the area of triangle $L M N$.
Give your answer correct to 3 significant figures.
. $\mathrm{cm}^{2}$
(a) Write $2 x^{2}-8 x+9$ in the form $a(x+b)^{2}+c$
(b) Hence, or otherwise, explain why the graph of the curve with equation $y=2 x^{2}-8 x+9=0$ does not intersect the $x$-axis.
$\qquad$
$\qquad$
$A B C D$ is a parallelogram.

$$
\overrightarrow{A B}=\binom{2}{3} \quad \overrightarrow{A C}=\binom{9}{4}
$$

Find the magnitude of $\overrightarrow{B C}$

24 Show that $\frac{\sqrt{12}-1}{2-\sqrt{3}}$ can be written as $4+3 \sqrt{3}$
Show your working clearly.

25 A particle moves along a straight line.
The fixed point $O$ lies on this line.
The displacement of the particle from $O$ at time $t$ seconds, $t \geq 0$, is $s$ metres, where

$$
s=t^{3}-5 t^{2}-8 t+3
$$

Find the value of $t$ for which the particle is instantaneously at rest.

$$
t=
$$

$\qquad$

